

Errors of mathematical processing: The time course of dorsolateral prefrontal and anterior cingulate cortex activity when solving algebra equations

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- ❖ Our goal was to assess regions important for successful mathematical problem-solving
- ❖ Prefrontal regions are more engaged when recognizing incorrect equations (e.g., $2 + 2 = 5$) (Menon, et al., 2002)
- ❖ However, no study has examined whether prefrontal activity is related to the production of correct solutions

Question 1: Will activity in prefrontal regions differ between correct and error trials?

- ❖ Regions of the anterior cingulate cortex (ACC) have been dissociated based on whether conceptual or response conflict is present (Van Veen & Carter, 2005)

- ❖ In this design, we assume that the problem solving phase should include both types of conflict whereas only response conflict should be present in the response stage

Question 2: Will dissociable regions of the ACC be active in the problem-solving and response phases?

- ❖ This is the first event-related study that examines number size effects
- ❖ We predict that regions associated with successful calculation regardless of number size are important for general problem-solving.

- ❖ Regions that are crucial for solving equations with large but not small numbers may be important for numerical manipulation and/or working memory.

Question 3: What regions are important for general problem-solving vs. regions that are engaged by greater numerical processing or working memory demands?

Subjects: n=9, average age = 23.8

Only subjects who achieved between 25% - 75% correct in pre-testing were included

Stimuli:

Small $(x - 6)/3 = 7$

Large $5 * (x - 7) = 65$

Procedure:

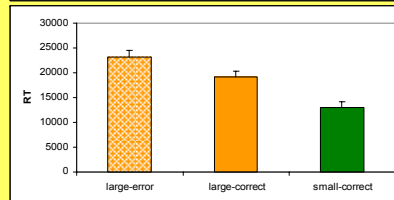
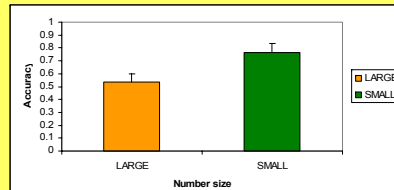
Participants had 40 s to solve the equation. When they had an answer, they pressed a key and then used their index and middle fingers to key in an answer.

Analyses:

- ❖ 7 – 9 runs of 12 trials each were acquired for each participant
- ❖ ROIs were obtained using a number size (2) x time (21) ANOVA or an accuracy x time (21) ANOVA. We were unable to include both accuracy and number size in an omnibus ANOVA because participants made too few errors in the small number condition.
- ❖ Voxel-wise tests used a threshold of $p < .001$ and a cluster size of 8 voxels

| | | | |
|------------|-----------------------|--------|---------|
| Type | EPI | Slices | 36 |
| Scanner | 3T Siemens Trio | TR | 2000 ms |
| Voxel size | 3.438 x 3.438 x 3.4mm | TE | 25 ms |
| Flip angle | 90 | FOV | 220 mm |

Behavioral Results



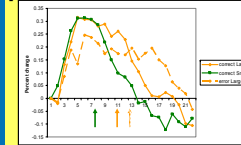
All conditions are significantly different from each other ($p < .005$)

METHODS

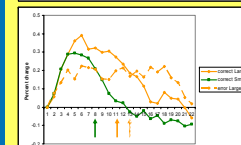
RESULTS

Accuracy x time

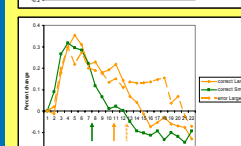
Errors are associated with reduced activity in the DLPFC & ACC during problem solving



BA 9 (38,26,33)



BA 9 (-45,23,29)



BA 32 (-11,17,44)

↑ ↑ ↑ = time of response in each condition

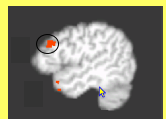
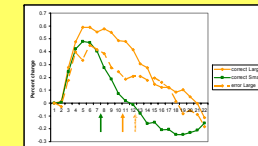
Other regions showing this pattern are the SMA, left BA 19, left thalamus, & right cerebellum

RESULTS

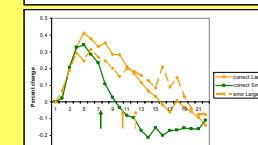
RESULTS

Number size x time

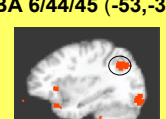
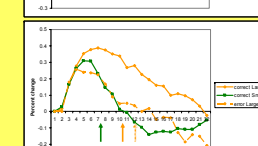
DLPFC, VLPFC, & parietal cortex are more active when correctly solving equations with large numbers



BA 9 (50,-23,29)



BA 6/44/45 (-53,-3,36)



BA 39 (31,-63,32)

RESULTS

DISCUSSION

- ❖ Question 1: DLPFC was more active when participants solved the equation correctly regardless of number size.

- ❖ Question 2: The region of the ACC previously associated with conceptual conflict was primarily active in the problem-solving phase whereas a more ventral region was active in both phases.

- ❖ Question 3: DLPFC and cingulate (and other regions) were important for general problem-solving whereas parietal, DLPFC, and VLPFC were specifically involved for correctly solving equations where numerical processing and working memory demands were high.

- ❖ These results constitute the first step in being able to relate errors in mathematical problem-solving with reduced neural function.

BA 6/32(6,26,36)

Caudate (21,10,25)